

Rationalizing Denominators

"Rational" refers to a number that is a ratio - that is, a number that ends at some point. Having a $\sqrt{\quad}$ in the denominator makes that number non-rational (irrational).

This is non-rational:

$$\frac{\sqrt{6}}{\sqrt{2}}$$

because of this guy

To make a number like this rational again, you need to get rid of the $\sqrt{\quad}$ in the denominator. To do this, multiply the top and bottom by the bottom:

$$\frac{\sqrt{6}}{\sqrt{2}} \left(\frac{\sqrt{2}}{\sqrt{2}} \right) \rightarrow \frac{\sqrt{6} \cdot \sqrt{2}}{\sqrt{2} \cdot \sqrt{2}}$$

When multiplying roots ~~w/ different #s~~, keep the $\sqrt{\quad}$ and multiply the numbers inside. When multiplying roots with the same # inside, square the root:

$$\frac{\sqrt{6} \cdot \sqrt{2}}{\sqrt{2} \cdot \sqrt{2}} \rightarrow \frac{\sqrt{6 \cdot 2}}{(\sqrt{2})^2} \rightarrow \boxed{\frac{\sqrt{12}}{2}}$$

← exponent cancels out of the same power